

Two-Phase Pressure Drop of Gas and Liquid Flowing in a Pipe

Pipe relative roughness and diameter

$$e := 0.0002 \quad d := 95.0 \text{ mm}$$

Cross-sectional area of pipe

$$A := \frac{\pi \cdot d^2}{4} = 7.088 \times 10^3 \text{ mm}^2$$

Colebrook equation

$$\text{friction} := (\text{Rey}, y) \text{ fsolve} \left(\frac{1}{\sqrt{f_{\text{turb}}}} = -2 \cdot \log_{10} \left(\frac{e}{3.7} + \frac{2.51}{\text{Rey} \cdot \sqrt{f_{\text{turb}}}} \right) \right)$$

Lockhart-Martinelli factor

$$X_{\text{tt}} := \sqrt{\frac{d\text{PdL}_L}{d\text{PdL}_G}}$$

Liquid

Gas

Mass flowrate

$$W_L := 17.0 \text{ kg} \cdot \text{s}^{-1}$$

$$W_G := 2.5 \text{ kg} \cdot \text{s}^{-1}$$

Viscosity

$$\mu_L := 0.003 \text{ Pa} \cdot \text{s}$$

$$\mu_G := 1.92 \times 10^{-5} \text{ Pa} \cdot \text{s}$$

Density

$$\rho_L := 880 \text{ kg} \cdot \text{m}^{-3}$$

$$\rho_G := 3 \text{ kg} \cdot \text{m}^{-3}$$

Liquid and gas mass fluxes

$$G_L := \frac{W_L}{A} = 2.398 \times 10^3 \frac{\text{kg}}{\text{s} \cdot \text{m}^2}$$

$$G_G := \frac{W_G}{A} = 352.698 \frac{\text{kg}}{\text{s} \cdot \text{m}^2}$$

Reynolds Number

$$\text{Rey}_L := \frac{G_L \cdot d}{\mu_L} = 7.595 \times 10^4$$

$$\text{Rey}_G := \frac{G_G \cdot d}{\mu_G} = 1.745 \times 10^6$$

Liquid and gas friction factor

$$f_L := \text{friction}(\text{Rey}_L, e) = 0.020$$

$$f_G := \text{friction}(\text{Rey}_G, e) = 0.014$$

Pressure gradient

$$d\text{PdL}_L := \frac{f_L}{2} \cdot \frac{G_L^2}{\rho_L \cdot d} = 686.119 \frac{\text{Pa}}{\text{m}}$$

$$d\text{PdL}_G := \frac{f_G}{2} \cdot \frac{G_G^2}{\rho_G \cdot d} = 3122.700 \frac{\text{Pa}}{\text{m}}$$

two-phase multiplier

$$\phi_L := \left(1 + 18 \cdot X_{\text{tt}}^{-1} + X_{\text{tt}}^{-2} \right)^{0.5} = 6.630$$

$$\phi_G := \left(1 + 18 \cdot X_{\text{tt}} + X_{\text{tt}}^2 \right)^{0.5} = 3.108$$