

El Centro Earthquake Data Analysis

▼ Introduction

This application analyzes the response of a SDOF to the 1940 El Centro earthquake. It uses acceleration data recorded from a seismograph located near the fault line

▼ Import and Visualize Data from Seismograph

```
> restart:  
with(SignalProcessing): with(plots):  
> NS := ImportMatrix("elcentro_NS.csv", source = csv[standard], datatype = float[8]);
```

$$NS := \begin{bmatrix} 2688 \times 2 \text{ Matrix} \\ \text{Data Type: } \text{float}_8 \\ \text{Storage: rectangular} \\ \text{Order: Fortran_order} \end{bmatrix} \quad (2.1)$$

Separate the data into time (in seconds) and acceleration (in g) components

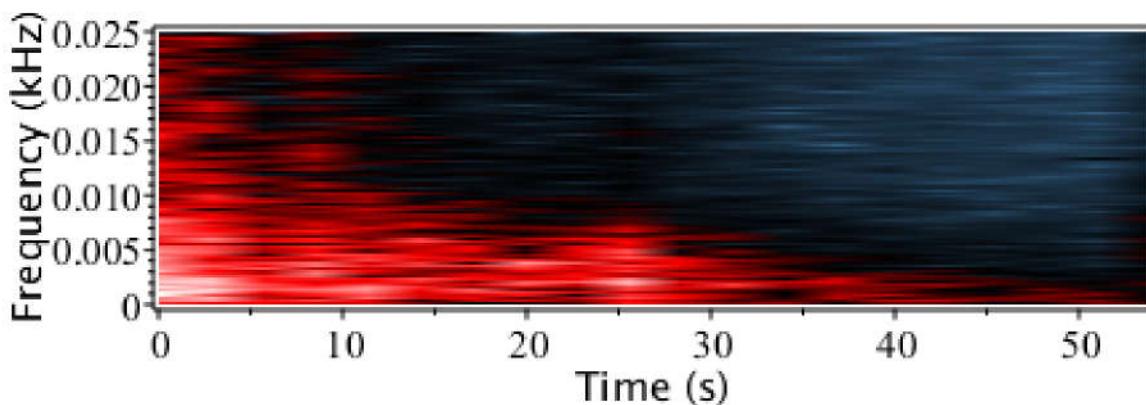
```
> t_NS := NS[.., 1]:  
acc_NS := NS[.., 2]:
```

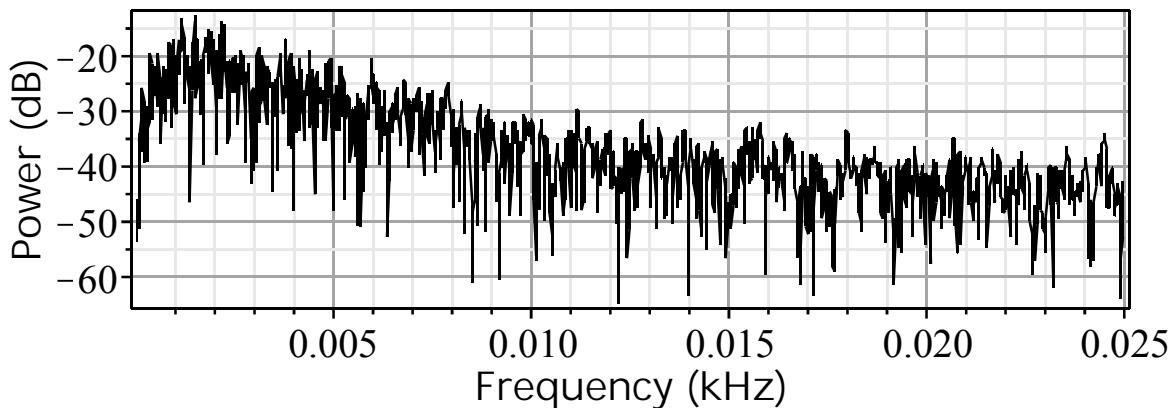
Sample rate of data

```
> sr :=  $\frac{1}{t_{NS}[2] - t_{NS}[1]}$   
sr := 50. \quad (2.2)
```

Plot a spectrogram and power spectrum

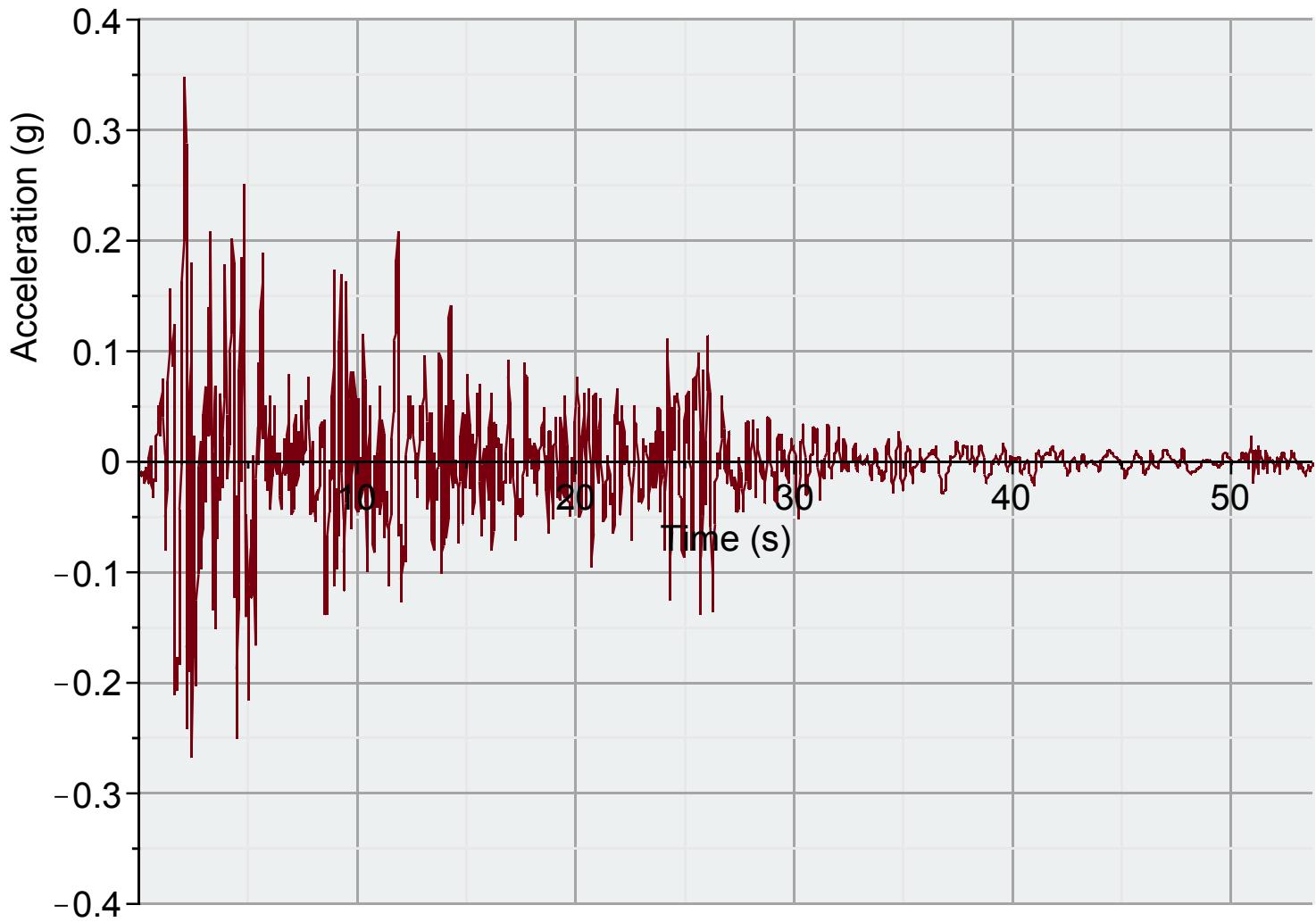
```
> Spectrogram(acc_NS, samplerate = 50, fftsize = 256, includepowerspectrum, colorscheme = ["zgradient",  
["SteelBlue", "black", red, white], markers = [0, 0.7, 0.85, 1]])
```





Plot the time history

```
> plot(t_NS, acc_NS, view = [default, -0.4 .. 0.4], labels = ["Time (s)", "Acceleration (g)", labelfont = [Arial], axesfont = [Arial], gridlines, size = [1200, 400], background = ColorTools:-Color("RGB", [236 / 255, 240 / 255, 241 / 255]), style = patchnogrid, thickness = 0)
```



Set the eigenperiod of an ideally zero-stiffness SDOF oscillator, in order to calculate the maximum velocity of the earthquake

▼ Displacement Response of a SDOF

```
> eq := \ddot{u} + 2\xi\cdot\omega_n\cdot\dot{u} + \omega_n^2\cdot u = -9.81 acc(t) :
```

$$> \omega_n := \frac{2\cdot\text{Pi}}{T_n} :$$

where ω_n is the natural frequency, and T_n is the natural period of vibration.

$$> \xi := 0.02 :$$

$$T_n := 5 :$$

$$> acc := \text{unapply}\left(\text{CurveFitting:-Spline}\left(t_NS, \frac{\text{acc_NS}}{9.81}, t, \text{degree} = 1\right), t\right) :$$

$$> res := \text{dsolve}(\{\text{eq}, u(0) = 0, D(u)(0) = 0\}, \text{numeric}, \text{maxfun} = 0) :$$

$$> \text{odeplot}\left(res, [t, u(t)], t = 0 .. 50, \text{labels} = ["Time (s)", "Displacement (m)"], \text{labelfont} = [\text{Arial}], \text{axesfont} = [\text{Arial}], \text{size} = [800, 500], \text{background} = \text{ColorTools:-Color}\left("RGB", \left[\frac{236}{255}, \frac{240}{255}, \frac{241}{255}\right]\right), \text{style} = \text{patchnogrid}, \text{thickness} = 0, \text{size} = [800, 500]\right)$$

